

## Scheduling with preemption delays: anomalies and issues

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## hard real-time scheduling

↔ common assumption for a long time: preemption costs = 0



## Context

## hard real-time scheduling

↪ common assumption for a long time: preemption costs = 0

- components off-the-shelf (COTS) in embedded systems:

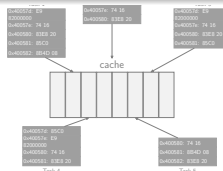
➤ CPU → fast,



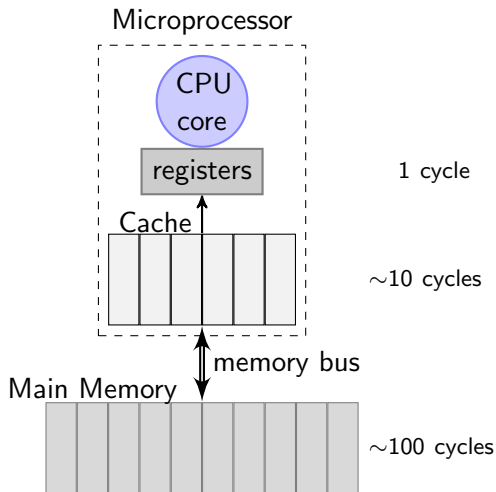
➤ **preemption cost as high as 44% of the task WCET**  
(Pellizzoni et al. 2007)

➤ **cache** → small

↪ potential bottleneck



## Cache-Related Preemption Delays (CRPDs)

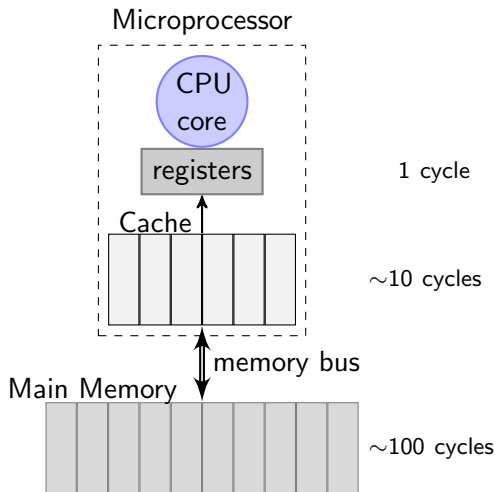


➤  $\text{cost}(\text{cache miss}) \gg \text{cost}(\text{cache hit})$

# Cache-Related Preemption Delays (CRPDs)

CRPD

**Additional reloads** because of  
cache evictions due to  
**preempting jobs**



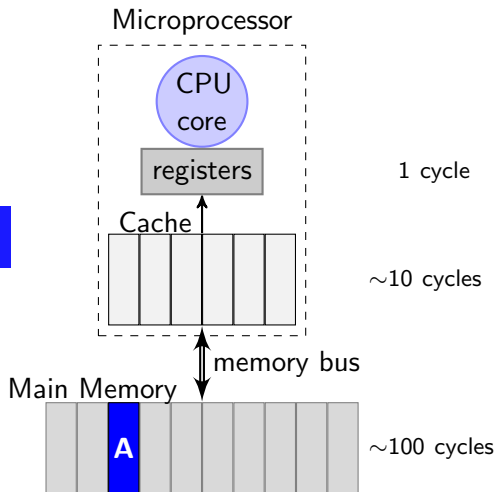
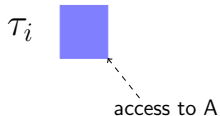
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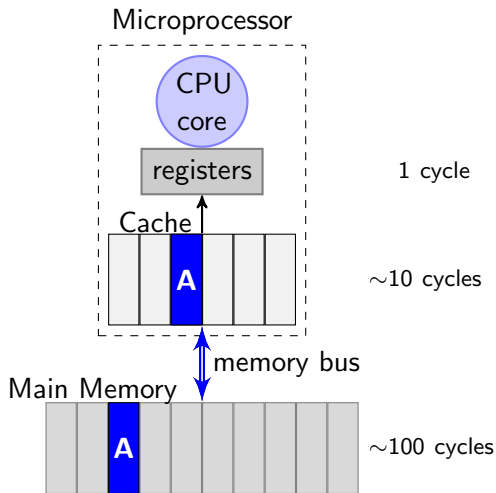
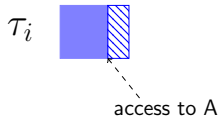


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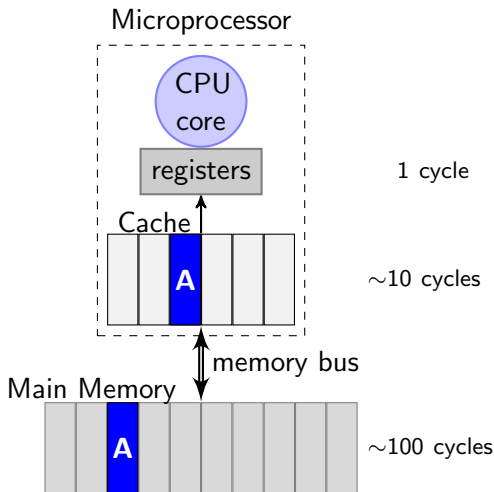
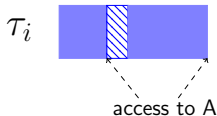


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HIT

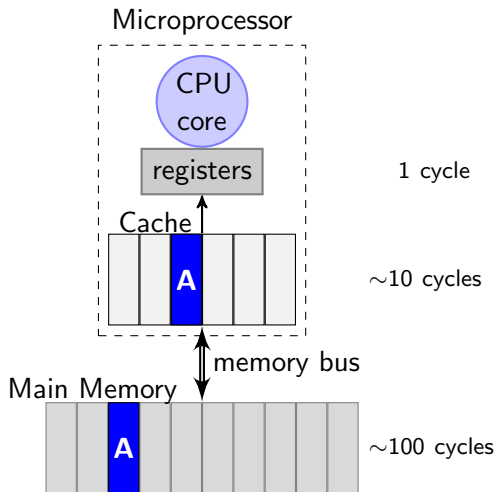
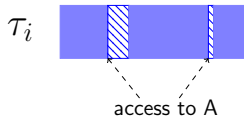


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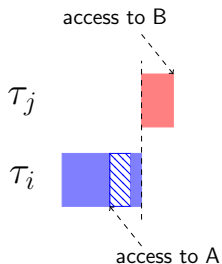


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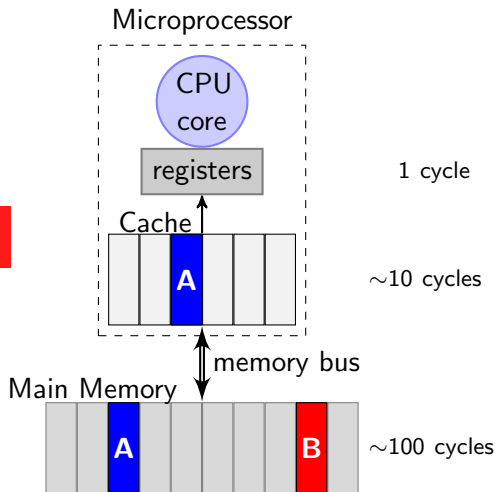
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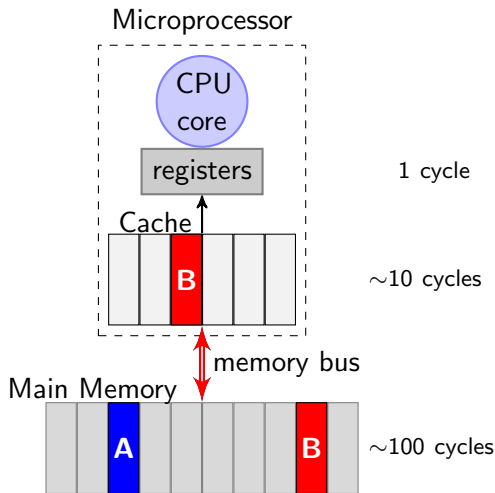
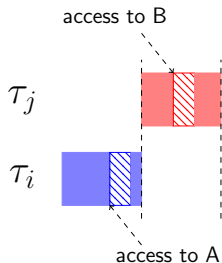


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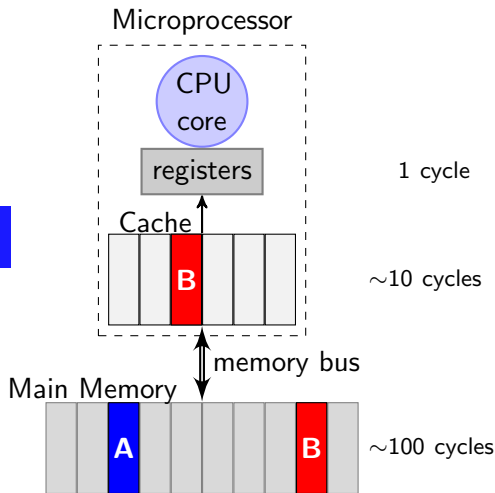
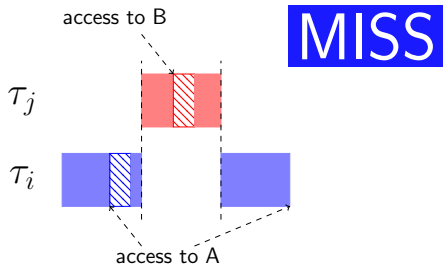


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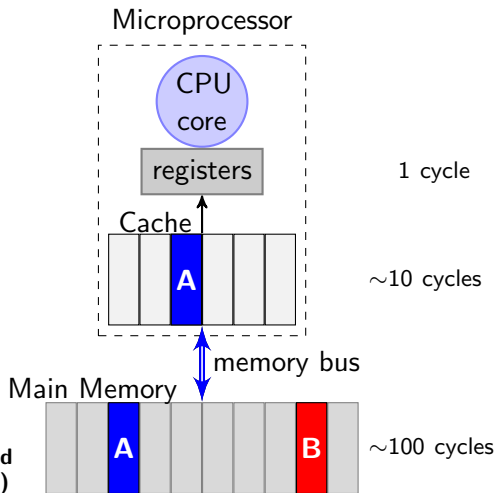
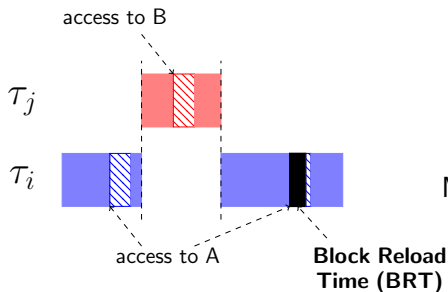


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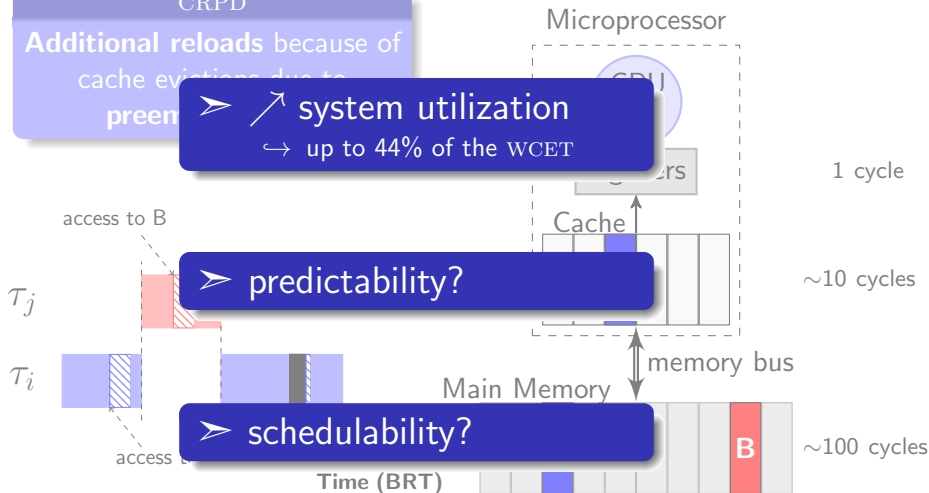
CRPD

Additional reloads because of  
cache evictions due to  
preemption

➤ ↗ system utilization  
↪ up to 44% of the WCET

➤ predictability?

➤ schedulability?



**Goal:**

Study the impact of CRPDs on hard real-time scheduling.

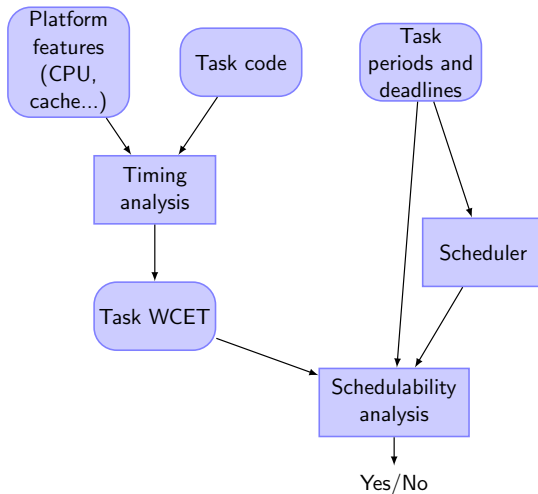
- **sustainability** of classic online scheduling policies subjected to CRPDs?
- **optimal** online CRPD-aware scheduling policy?
- **loss of schedulability** of classic online scheduling policies subjected to CRPDs?



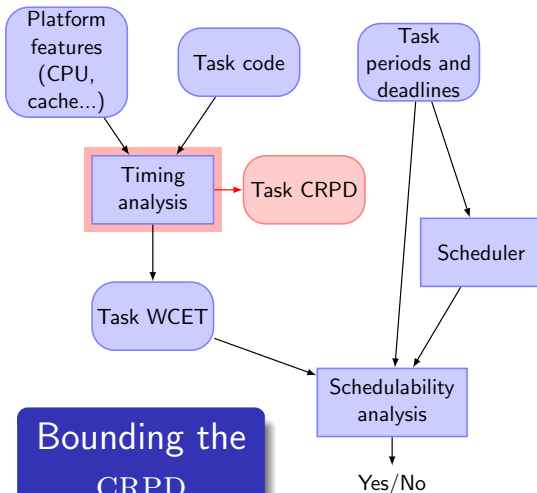
# Related Work

- 1 Introduction
- 2 Related Work**
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# CRPDs in real-time scheduling

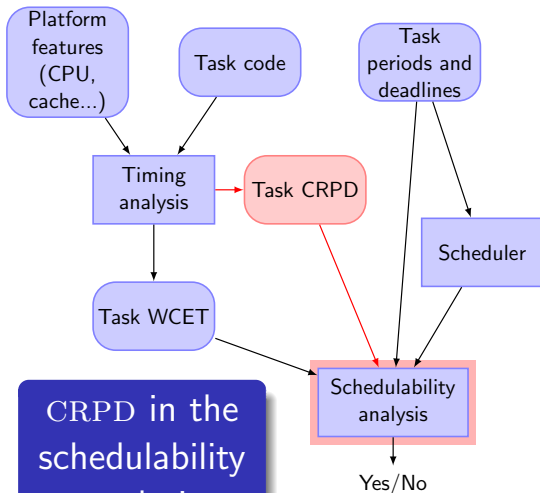


# CRPDs in real-time scheduling



- preempted task  
(*Lee et al. 1997*)
- preempting task  
(*Busquets-Mataix et al. 1996*)
- combined approaches  
(*Altmeyer et al. 2012*)

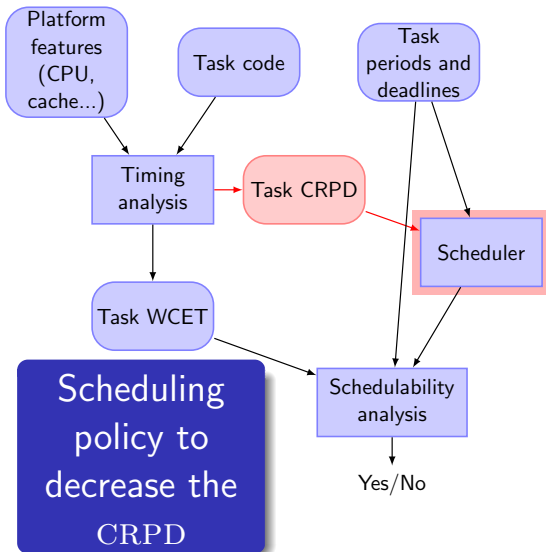
# CRPDs in real-time scheduling



CRPD in the  
schedulability  
analysis

- FP scheduling → Response Time Analysis (*Busquets-Mataix et al. 1996*)
- EDF → Demand Bound Function (*Lunniss et al. 2013*)

# CRPDs in real-time scheduling



- FPP placement  
(*Bertogna et al. 2011*)
- optimal CRPD-aware scheduling:
  - ↪ NP-hard in the strong sense  
(*Phavorin et al. 2015*)

# Online scheduling with CRPDs

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# CRPD-aware task model

## Periodic synchronously released tasks

$\tau_i(C_i, D_i, T_i, \gamma_i)$ :

- $C_i$ : WCET without CRPD  
 ↪  $\tau_i$  executed fully non preemptively
- $T_i$ : period
- $D_i$ : relative deadline  
 ↪ implicit deadline  $D_i = T_i$  or constrained deadline  $D_i \leq T_i$
- $\gamma_i$ : CRPD paid by  $\tau_i$  each time it resumes its execution after a preemption  
 ↪ max. delay for every possible preemption point in the task code

→ infinite sequence of jobs:  $\tau_{ij}(r_{ij} = (j - 1) \cdot T_i, C_i, d_{ij} = r_{ij} + D_i, \gamma_i)$

# Known results

## Online scheduling with CRPDs:

- EDF and FP scheduling algorithms (RM, DM)  $\rightarrow$  not optimal  
(*Phavorin et al. 2015*)
- for FP scheduling: synchronous releases  $\rightarrow$  not necessarily the critical instant worst-case scenario  
(*Ramaprasad et al. 2006, Meumeu et al. 2007*)



**Sustainability:** (*Burns et al. 2008*)

A scheduling policy is *sustainable* if any system deemed schedulable remains schedulable if:

- a WCET is decreased
- a period is increased
- a relative deadline is increased

Online scheduling **without** CRPD:

- EDF  $\rightarrow$  w.r.t: WCET, deadline, period
- FP scheduling policies (RM, DM)  $\rightarrow$  sustainable w.r.t.: WCET, deadline BUT NOT period

### Sustainability:

A scheduling policy is *sustainable* if any system deemed schedulable remains schedulable if:

- a WCET is decreased
- a period is increased
- a relative deadline is increased
- **a CRPD is decreased**

Online scheduling **without** CRPD:

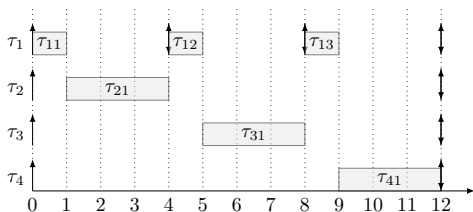
- I **Online scheduling with CRPDs**
- I  $\Rightarrow$  EDF and FP scheduling **NOT SUSTAINABLE** WCET,  
deadline BUT NOT period

# Sustainability w.r.t the WCET

$\tau_i(C_i, D_i, T_i, \gamma_i)$ :

- $\tau_1(1, 4, 4, 0.6)$ ,  $\tau_2(3, 12, 12, 0.6)$ ,  $\tau_3(3, 12, 12, 0.6)$ ,  $\tau_4(2, 12, 12, 0.6)$

↪ EDF, RM, DM → same job priority assignment (task index as tie breaker).



→ schedule with  $C_2 = 3$

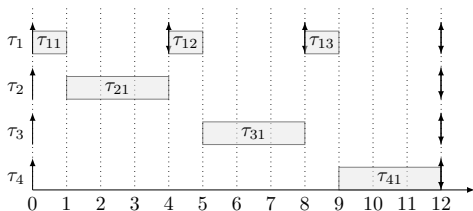
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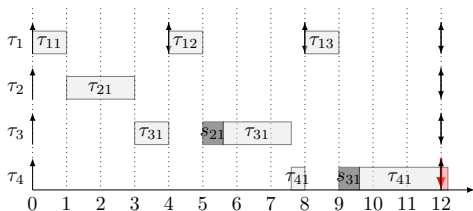
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➤ ↘ 1 task execution time ( $C_2 = 3 \rightarrow C_2 = 2$ )



→ schedule with  $C_2 = 3$



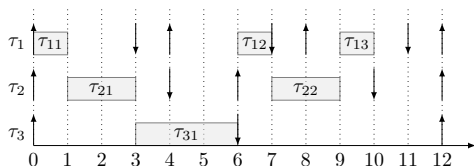
→ schedule with  $C_2 = 2$

# Sustainability w.r.t the deadline

$\tau_i(C_i, D_i, T_i, \gamma_i)$ :

- $\tau_1(1, 3, 4, 1)$ ,  $\tau_2(2, 4, 6, 1)$ ,  $\tau_3(3, 6, 12, 1)$

↪ EDF → same job priority assignment (task index as tie breaker).



→ EDF schedule with  $D_3 = 6$

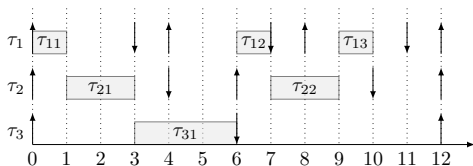
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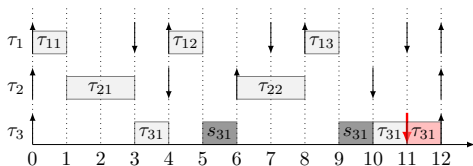
- $\tau_1(1, 3, 4, 1)$ ,  $\tau_2(2, 4, 6, 1)$ ,  $\tau_3(3, 6, 12, 1)$

↪ EDF → same job priority assignment (task index as tie breaker).

➤ ↗ 1 task relative deadline ( $D_3 = 6 \rightarrow D_3 = 11$ )



→ EDF schedule with  $D_3 = 6$



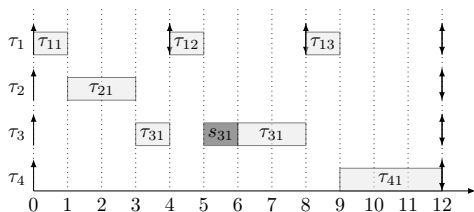
→ EDF schedule with  $D_3 = 11$

# Sustainability w.r.t the CRPD

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→ schedule with  $\gamma_3 = 1$

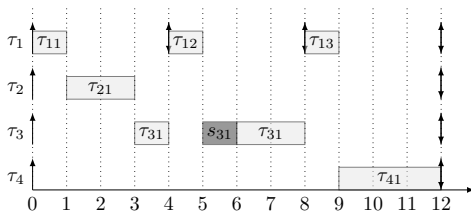
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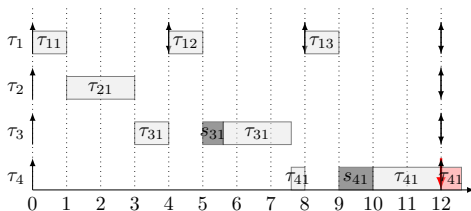
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↪ EDF, RM, EDF → same job priority assignment (task index as tie breaker).

➤ ↘ 1 task CRPD ( $\gamma_3 = 1 \rightarrow \gamma_3 = 0.6$ )



→ schedule with  $\gamma_3 = 1$



→ schedule with  $\gamma_3 = 0.6$



# Online scheduling of a set of jobs



- Online scheduling model:
  - set of jobs released over time
  - at each job release, all its parameters are known

→ *optimal online scheduling policy?*

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- Online scheduling model:
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**Result: Optimal online scheduling is impossible**

Job release times need to be known a priori to define an optimal online scheduler (i.e., clairvoyant).

# Proof

## Proof sketch

Optimal offline scheduler (a.k.a. the adversary) generates jobs so that any online scheduler cannot define a feasible schedule whereas the adversary can.

Jobs:  $\tau_1(0,5,12,1)$ ,  $\tau_2(4,5,10,1)$   $\rightarrow$  scheduling decision at  $t = 4$

### Adversary strategy:

➤ At time 4:

Case 1: the online scheduler **continues** to execute  $\tau_1$   
 $\hookrightarrow$  the adversary generates a new job  $\tau_3(9,1,10,1)$

Case 2: the online scheduler **preempts**  $\tau_1$  to execute  $\tau_2$   
 $\hookrightarrow$  the adversary generates a new job  $\tau_3(10,1,11,1)$

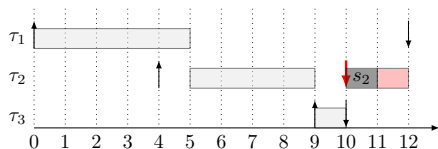
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**Case 1.** The online scheduler continues to execute job  $\tau_1$  at time 4. Adversary generates a job  $\tau_3(9,1,10,1)$ .



$\rightarrow$  Online algorithm

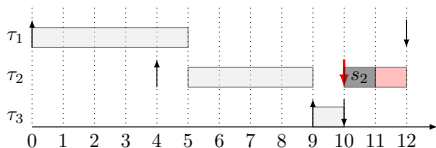
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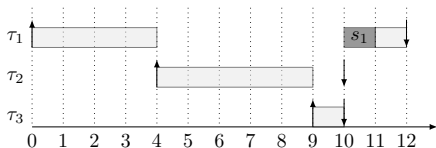
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$\rightarrow$  Adversary's feasible schedule

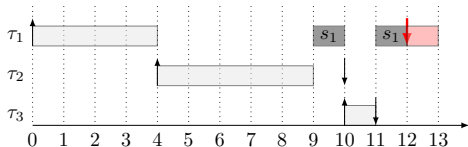
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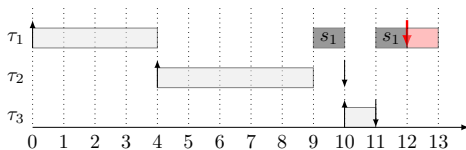
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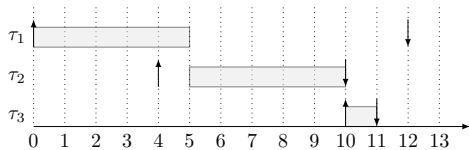
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# Offline scheduling



- set of tasks  $\tau_i(C_i, D_i, T_i, \gamma_i)$ 
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→ **Mixed Integer Linear Program (MILP) formulation**

**Objective function** → define an offline schedule to:

- minimize the total workload
- *or equivalently*, minimize the total CRPD (since the WCET contributes as a constant in the objective function)

# MILP formulation

## Schedule construction:

- schedule:
  - finite set of slices  $S_j$ ,
  - separated by releases/deadlines
  - ⇒ no job release inside a slice
- in every slice:
  - job-piece execution times + related CRPDs must fit in the slice interval

Every job resumes at most once  
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## MILP formulation



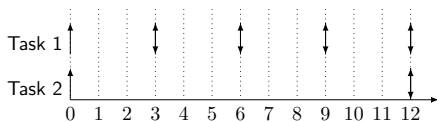
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- Task 1 (1,3,3,0.2)
- Task 2 (7,12,12,0.5)



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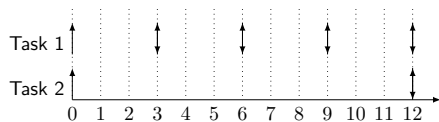
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- Task 2 (7,12,12,0.5)



slice
1
1
2
2
3
3
4
4

→ 4 Slices:

- ↪  $S_1 = [0, 3)$
- ↪  $S_2 = [3, 6)$
- ↪  $S_3 = [6, 9)$
- ↪  $S_4 = [9, 12)$

# MILP formulation

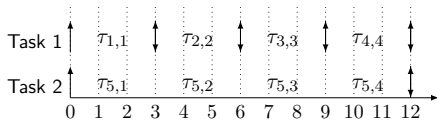
## Schedule construction:

- schedule:
  - finite set of slices  $S_j$ ,
  - separated by releases/deadlines
  - ⇒ no job release inside a slice
- in every slice:
  - job-piece execution times + related CRPDs must fit in the slice interval

Every job resumes at most once in every slice.

Exple: 2 periodic tasks within  $[0,12]$

- Task 1 (1,3,3,0.2)
- Task 2 (7,12,12,0.5)



slice	job
1	$\tau_1$
1	$\tau_5$
2	$\tau_5$
2	$\tau_2$
3	$\tau_3$
3	$\tau_5$
4	$\tau_5$
4	$\tau_4$

→ 4 Slices:

↪  $S_1 = [0, 3]$

↪  $S_2 = [3, 6]$

↪  $S_3 = [6, 9]$

↪  $S_4 = [9, 12]$

→ 8 job-pieces

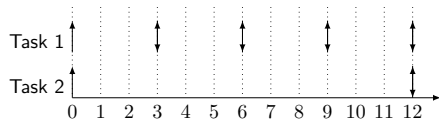
# MILP formulation

## Schedule construction:

- MILP variables for each slice  $S_j$ :
  - $t_{i,j} \in \mathbb{R} \rightarrow$  starting time of job-piece  $\tau_i$  in  $S_j$
  - $p_{i,j} \in \mathbb{R} \rightarrow$  execution time of job-piece  $\tau_i$  in  $S_j$
  - $\Delta_{i,j} \in \{0, 1\} \rightarrow$  job-piece has to pay a CRPD in  $S_j$ .

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3	$\tau_5$			
4	$\tau_5$			
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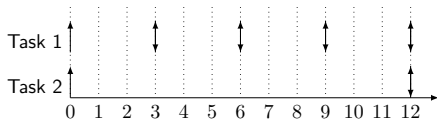
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## Constraints $\rightarrow$ construct a valid schedule:

- each job is executed for its WCET
- each job is executed between its release and its deadline
- at most one job is executed at any time instant

job	slice	$t_{i,j}$	$p_{i,j}$	$\Delta_{i,j}$
1	$\tau_1$	0	1	0
1	$\tau_5$	1	2	0
2	$\tau_5$	3	2	0
2	$\tau_2$	5	1	0
3	$\tau_3$	6	1	0
3	$\tau_5$	7.5	1	1
4	$\tau_5$	9	2	0
4	$\tau_4$	11	1	0



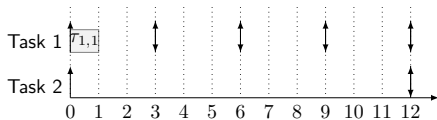
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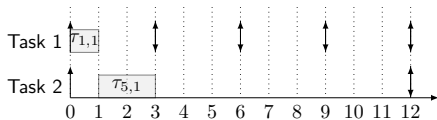
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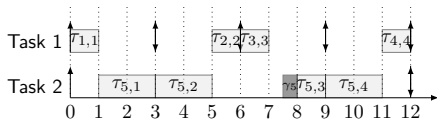
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# Evaluation

- 1 Introduction
- 2 Related Work
- 3 Online scheduling with CRPDS
  - Sustainability analyses
  - Optimal online scheduling
- 4 An offline solution
- 5 Evaluation**
  - Results
- 6 Conclusion

**Goal:**

Evaluate the loss of schedulability of classic online scheduling policies.

# Experiments

## Goal:

Evaluate the loss of schedulability of classic online scheduling policies.

- Synthetic tasksets:

- $C_i, T_i \rightarrow$  UUnifast (*Bini et al. 2005*)
  - ↪ to generate processor utilization factors
- $\gamma_i \rightarrow$  maximum CRPD Factor (PDF): % of  $C_i$ 
  - ↪  $\gamma_i = \text{PDF} \times C_i$
- limited to 200 jobs over the hyperperiod
  - ↪ to limit the MILP solving time

- Monitored algorithms:

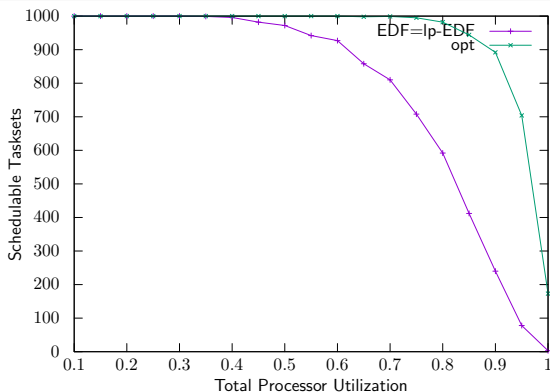
- EDF: arbitrary tie breaker
  - LP-EDF: tie breaker avoiding unnecessary preemptions
  - OPT: MILP solved using CPLEX 12.6.1
- } EDF schedulability analysis  
→ *Lunniss et al. 2013*

# Schedulability



## Experiment parameters:

- maximum CRPD Factor (PDF) = 20%,
- # of schedulable tasksets as a function of the total processor utilization.

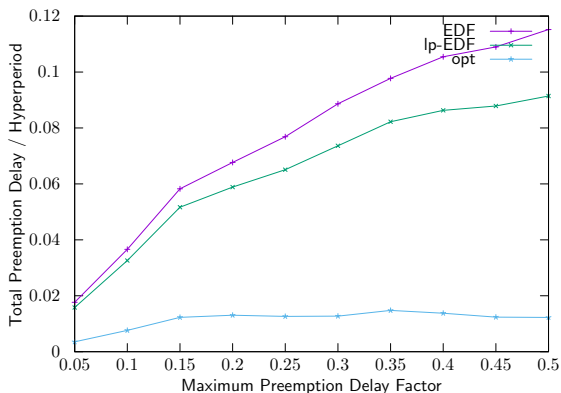


# Total CRPD



## Experiment parameters:

- Total Processor Utilization = 0.8,
- Total CRPD over the hyperperiod as a function of maximum PDF.





- **Conclusions:**
  - scheduling with CRPD → several issues:
    - classic policies (EDF, RM, DM) **not sustainable**
    - **no optimal** online scheduling policy
  - optimal offline scheduling using a MILP formulation
    - evaluation of schedulability loss for EDF

# Conclusions and Future Work

- **Conclusions:**

- scheduling with CRPD → several issues:
  - classic policies (EDF, RM, DM) **not sustainable**
  - **no optimal** online scheduling policy
- optimal offline scheduling using a MILP formulation
  - evaluation of schedulability loss for EDF

- **Future work:**

- evaluation of schedulability loss for other policies/techniques
- MILP with a more accurate CRPD parameter → **DIFFICULT**
- online scheduling using heuristics

**Thank you!**  
**Questions?**