

Static CRPD-Aware Real-Time Scheduling

ECRTS-WiP

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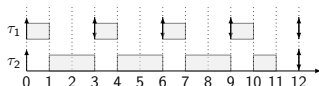
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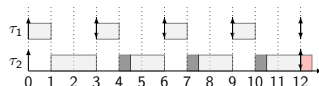
Actual platforms: CPUs + caches

⇒ **Cache-Related Preemption Delays (CRPD)**

→ cannot be neglected



→



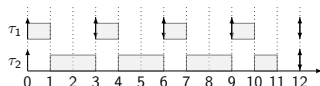
→ WCET depends on tasks running concurrently
(inter-task interference in the cache)

⇒ WCETs are not independent

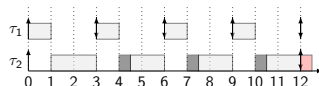
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- *preemption-aware scheduling*: preemption thresholds, deferred preemption, preemption points...
- *CRPD-aware scheduling* → scheduling decisions using CRPD values

CRPD-aware scheduling problem

$\tau_i(C_i, T_i, D_i, s_i)$

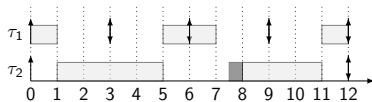
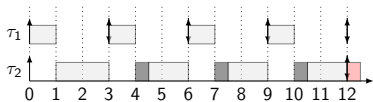
- additional task parameter $\rightarrow s_i$: worst-case CRPD for τ_i
- C_i : WCET without CRPD

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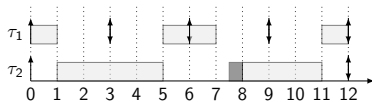
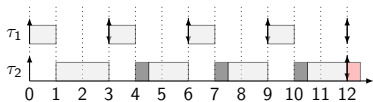


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\rightarrow **NP-hard** in the strong sense

A solution using static scheduling

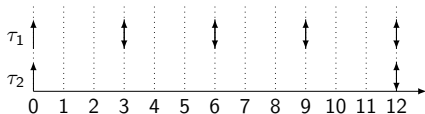
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- mathematical problem → Mixed-Integer Linear Program (MILP)
 - schedule → set of slices delimited by releases and deadlines

$\tau_1(1, 3, 3, 0.25)$	$J_1(0, 1, 3, 0.25)$	$J_{1,1} \in [0, 3)$
	$J_2(3, 1, 6, 0.25)$	$J_{2,2} \in [3, 6)$
	$J_3(6, 1, 9, 0.25)$	$J_{3,3} \in [6, 9)$
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$\tau_2(7, 12, 12, 0.5)$	$J_5(0, 7, 12, 0.5)$	$J_{5,1} \in [0, 3)$
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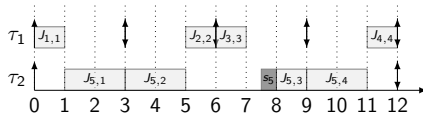


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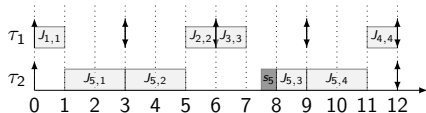


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- objective function → minimize the overall CRPD
 - under several constraints:
 - every job-piece executed in its slice
 - only one job-piece executed at a time
 - CRPD when another job-piece scheduled between 2 job-pieces of a same job
- full MILP in the paper

- evaluate on-line scheduling policies (RM,EDF...)
 - loss of schedulability
 - number of preemptions
- extend the mathematical problem to take into account improved cache analysis (preempted + preempting tasks)
- devise online heuristics scheduling algorithms

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