

Complexity of scheduling real-time tasks subjected to cache-related preemption delays

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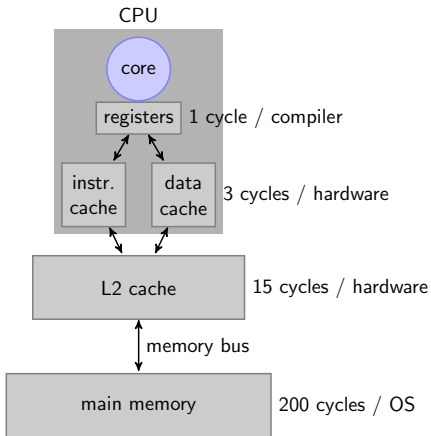
Context

- more and more embedded applications
- ↗ processing needs
- use of Component off-the-shelf (COTS) → **cache**

Context

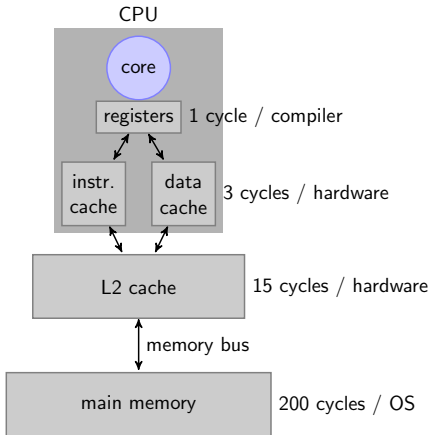
- more and more embedded applications
- ↗ processing needs
- use of Component off-the-shelf (COTS) → **cache**
- **hard real-time scheduling** → usually: $\text{preemption costs} = 0$
 - ↪ still valid with cache?

Cache

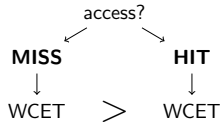


- bridge the gap between the CPU speed and the main memory access time
- $\text{cost}(\text{cache miss}) \gg \text{cost}(\text{cache hit})$

Cache



- bridge the gap between the CPU speed and the main memory access time
- $\text{cost}(\text{cache miss}) \gg \text{cost}(\text{cache hit})$
- *General assumptions:*
 - only one instruction cache
 - no timing anomaly:



Cache-Related Preemption Delays (CRPD)

CRPD

Additional reloads because of
cache evictions due to
preempting jobs

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CRPD

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cache



MISS

τ_i



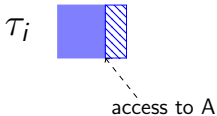
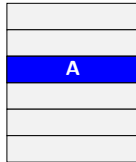
access to A

Cache-Related Preemption Delays (CRPD)

CRPD

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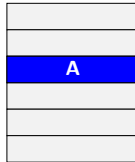


Cache-Related Preemption Delays (CRPD)

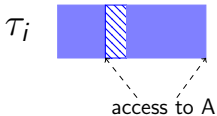
CRPD

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HIT

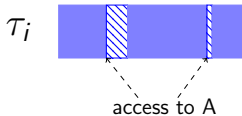
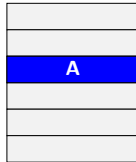


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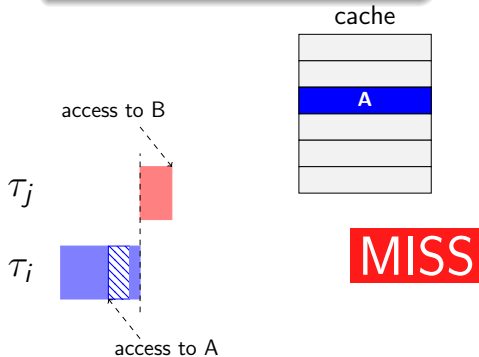
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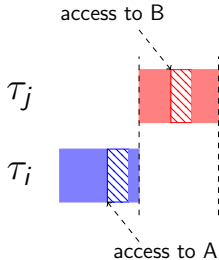
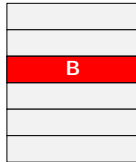


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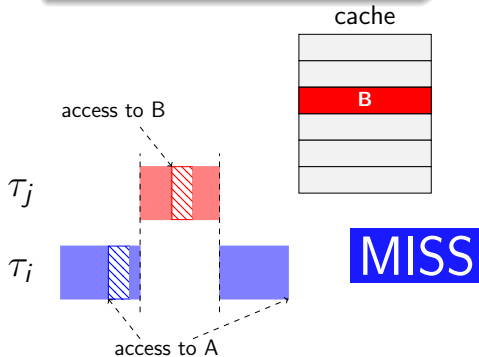
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Cache-Related Preemption Delays (CRPD)

CRPD

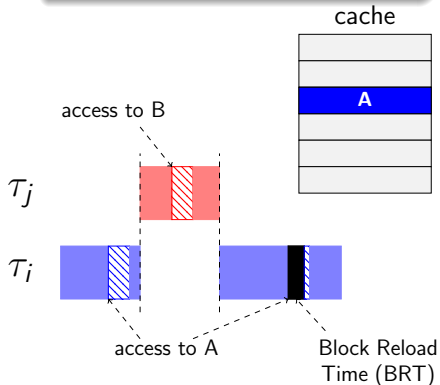
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Cache-Related Preemption Delays (CRPD)

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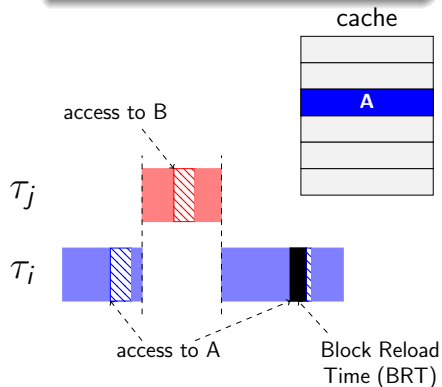


Cache-Related Preemption Delays (CRPD)

CRPD

Additional reloads because of cache evictions due to preempting jobs

➤ ↗ WCET

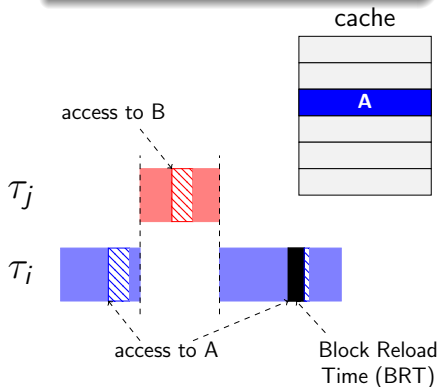


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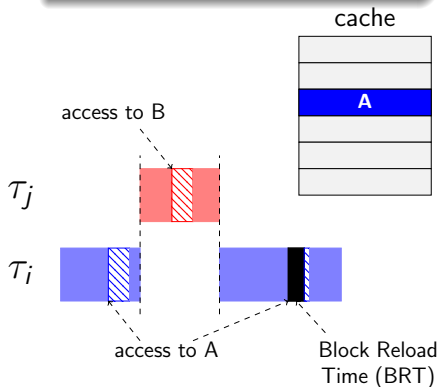
➤ predictability?



Cache-Related Preemption Delays (CRPD)

CRPD

Additional reloads because of cache evictions due to preempting jobs



➤ ↗ WCET

➤ predictability?

➤ schedulability?

Outline

Goals:

- studying the problem of scheduling hard real-time tasks subjected to cache-related preemption delays
- studying the complexity of taking scheduling decisions based on cache-related constraints

1 Related work

2 Scheduling problems

- CRPD-aware scheduling problem
- Cache-aware scheduling problem

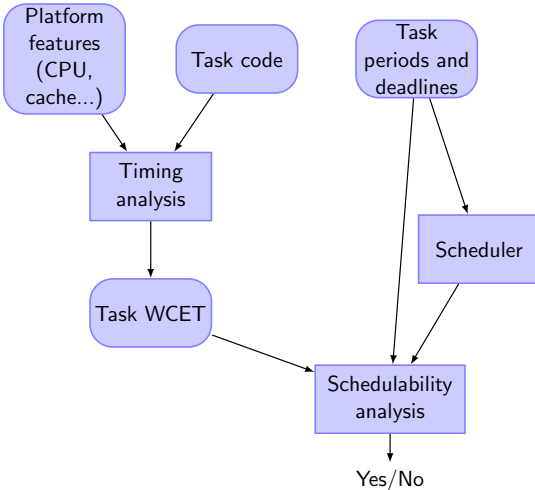
3 Conclusion

- Future works

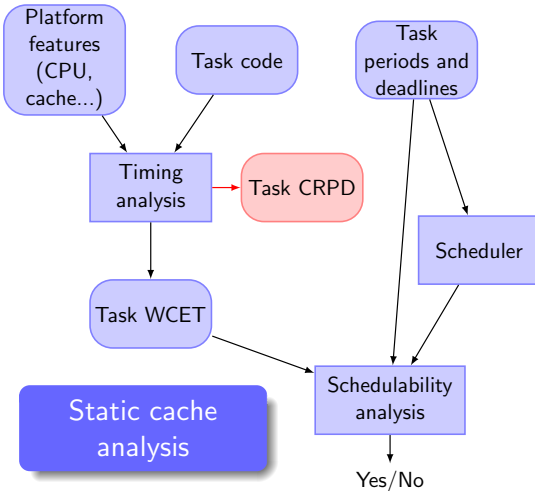
Related work

- 1 Related work
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Bounding the CRPD



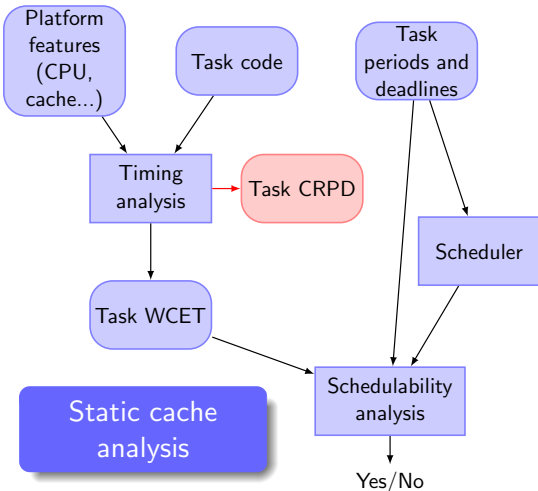
Bounding the CRPD



- preempted task
 - ↳ Useful Cache Blocks (UCBs)

- Lee et al., “Enhanced analysis of cache-related preemption delay in fixed-priority preemptive scheduling”

Bounding the CRPD

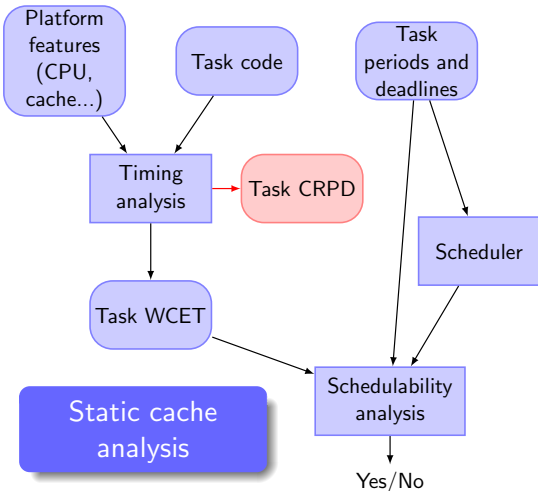


- preempted task
 - ↳ Useful Cache Blocks (UCBs)

- preempting task
 - ↳ Evicting Cache Blocks (ECBs)

- *Busquets-Mataix et al., "Adding instruction cache effect to schedulability analysis of preemptive real-time systems"*

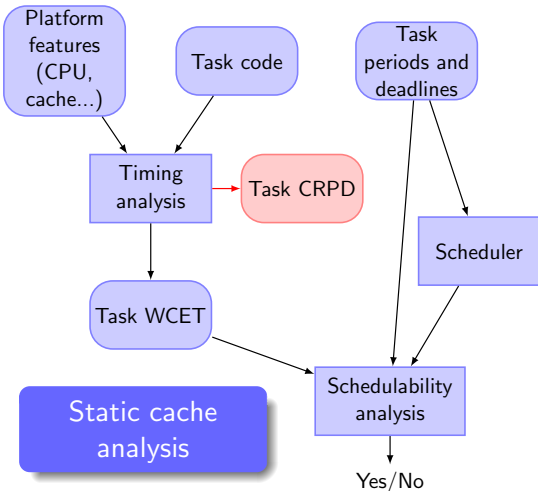
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- preempted task
 - ↳ Useful Cache Blocks (UCBs)
- preempting task
 - ↳ Evicting Cache Blocks (ECBs)
- combined approaches
 - ↳ both tasks

- Altmeyer, Davis, and Maiza, "Improved cache related pre-emption delay aware response time analysis for fixed priority pre-emptive systems"

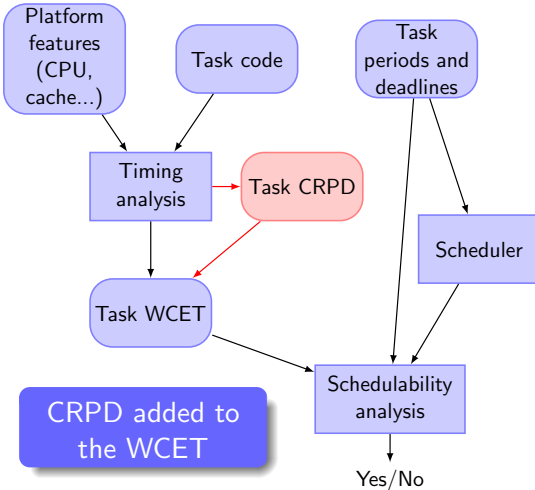
Bounding the CRPD



- preempted task
 - ↪ Useful Cache Blocks (UCBs)
- preempting task
 - ↪ Evicting Cache Blocks (ECBs)
- combined approaches
 - ↪ both tasks
- improvements:
 - ↪ Definitely-Cached UCBs

- Altmeyer and Maiza-Burguière, "A New Notion of Useful Cache Block to Improve the Bounds of Cache-Related Preemption Delay"

Bounding the CRPD



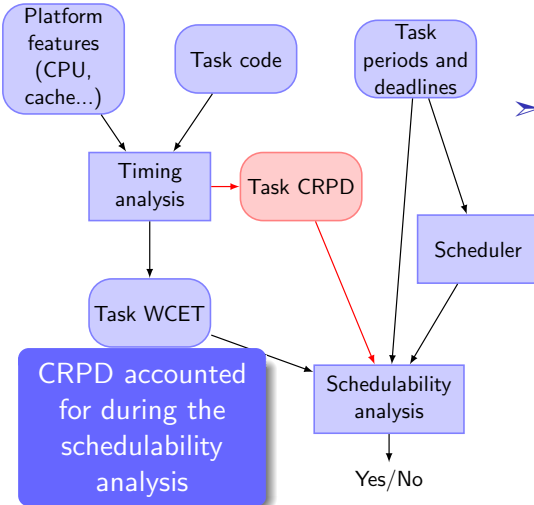
$$\triangleright \text{WCET}_{\text{w/o preemption}} + n \times \text{CRPD}$$

$$\hookrightarrow n?$$

CRPD added to the WCET

- Altmeyer and Burguière, "Cache-related preemption delay via useful cache blocks: Survey and redefinition"

Bounding the CRPD

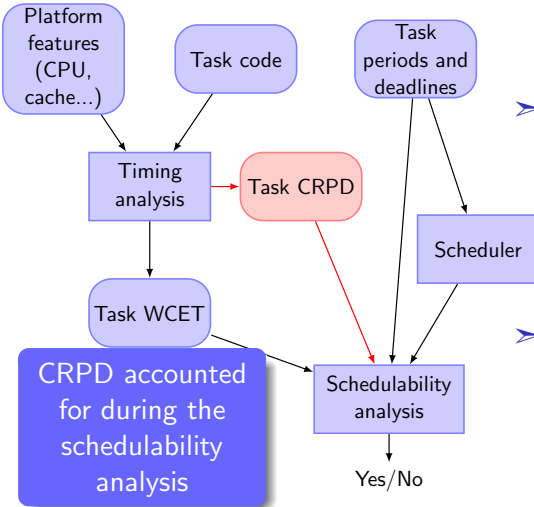


➤ Response Time Analysis:

$$\hookrightarrow R_i = C_i + \sum \left\lceil \frac{R_i}{T_j} \right\rceil \cdot (C_j + \gamma_{i,j})$$

➤ *Busquets-Mataix et al., "Adding instruction cache effect to schedulability analysis of preemptive real-time systems"*

Bounding the CRPD



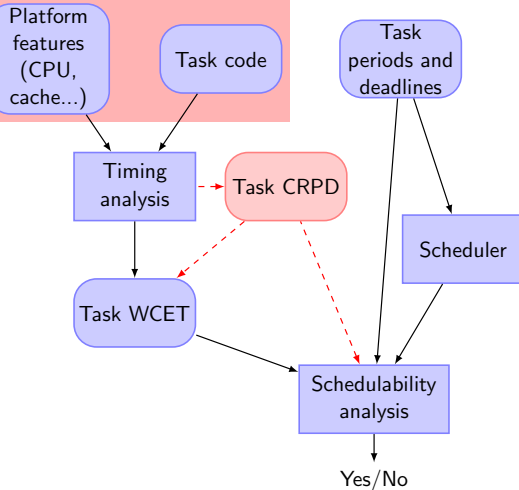
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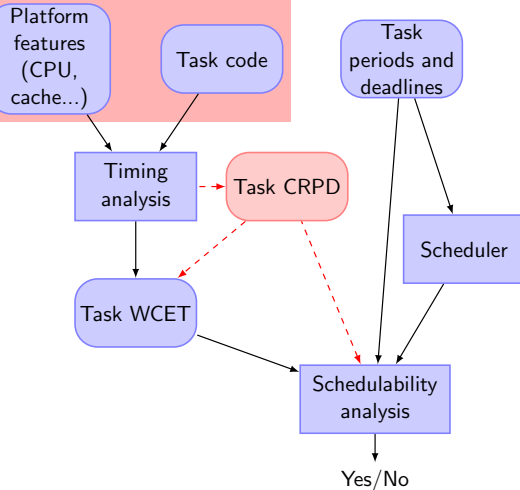
➤ EDF → time demand analysis.

➤ Lunniss et al., "Integrating cache related pre-emption delay analysis into EDF scheduling"

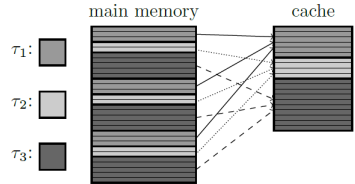
Cache management



Cache management

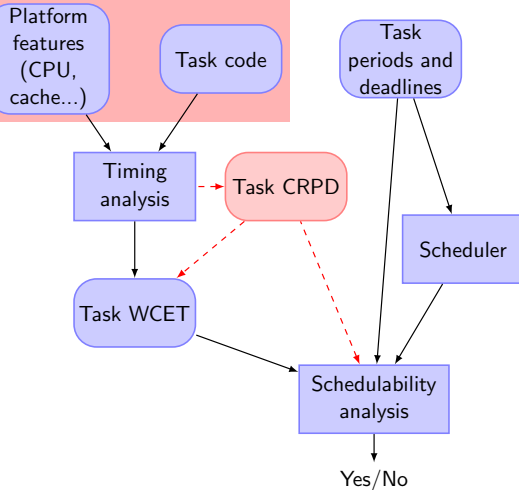


➤ cache partitioning



➤ Bui et al., "Impact of cache partitioning on multi-tasking real time embedded systems"

Cache management



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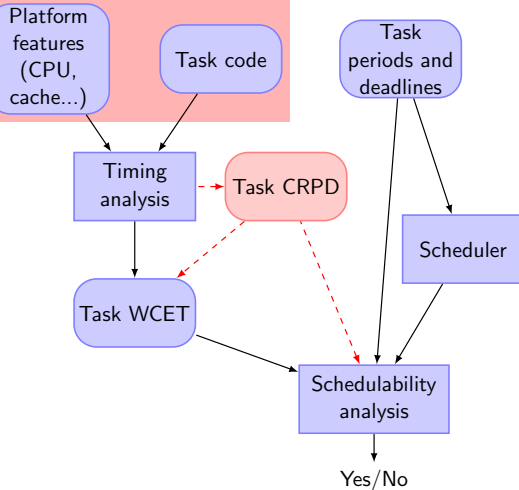
➤ cache locking

→ cache content fixed

⇒ predictability

➤ Ding, Liang, and Mitra, "Integrated Instruction Cache Analysis and Locking in Multitasking Real-time Systems"

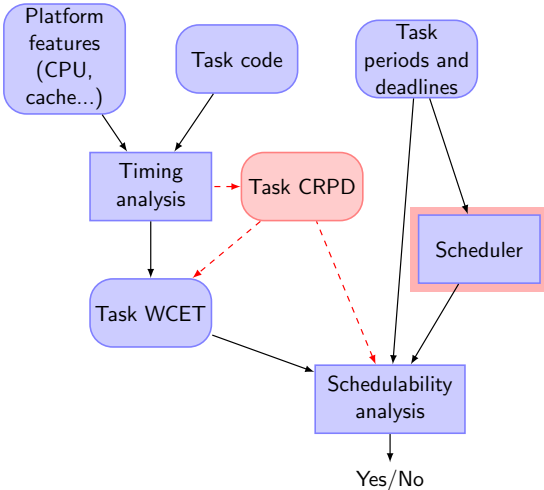
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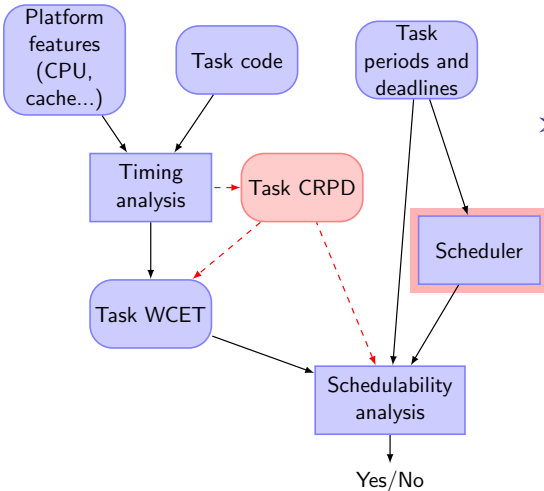
- cache partitioning
- cache locking
 - cache content fixed
 - ⇒ predictability
- memory layout
 - code positioning
 - ⇒ ↘ WCET
 - task positioning
 - ⇒ ↘ CRPD

- Lunniss, Altmeyer, and Davis, "Optimising Task Layout to Increase Schedulability via Reduced Cache Related Pre-emption Delays"

Schedulability



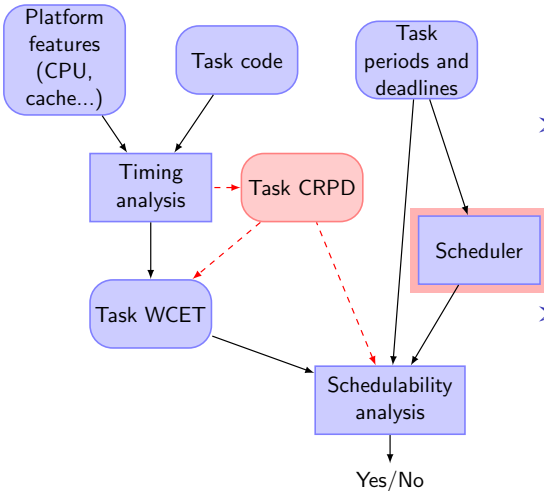
Schedulability



- preemption thresholds
 - ↳ preemption possible only if:
 $\text{priority}(\text{preempting task}) > \text{threshold}(\text{preempted task})$

- *Bril et al., "Integrating Cache-Related Pre-Emption Delays into Analysis of Fixed Priority Scheduling with Pre-Emption Thresholds"*

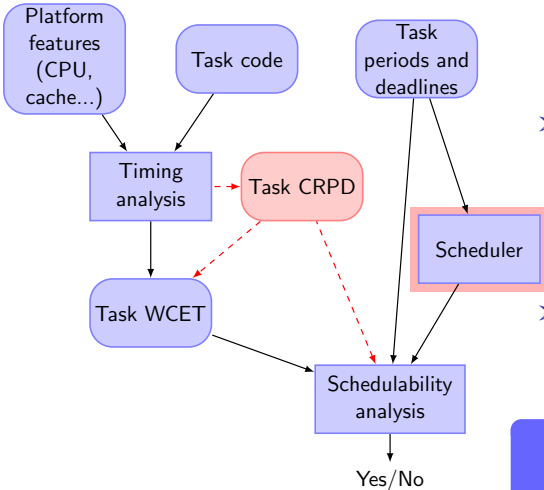
Schedulability



- preemption thresholds
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- deferred preemptions
 - ↳ preemption postponed as much as possible

➤ Bertogna and Baruah, "Limited Preemption EDF Scheduling of Sporadic Task Systems"

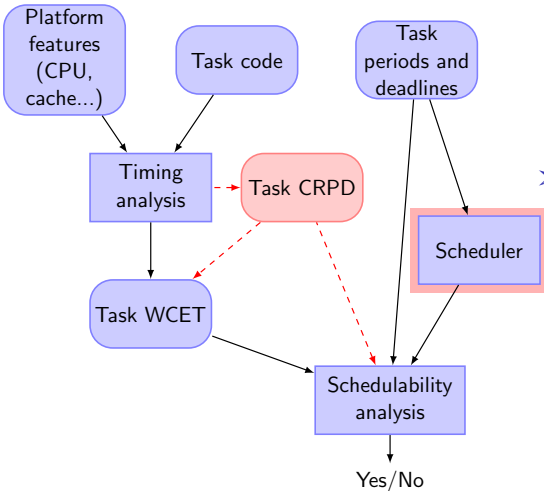
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Scheduling decisions are not directly based on a CRPD parameter.

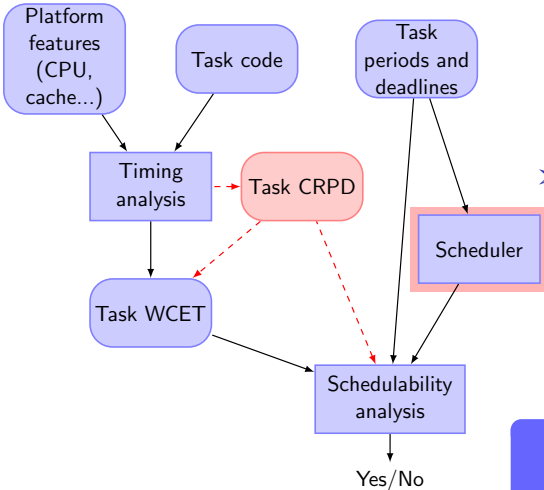
Schedulability



- Fixed Preemptive Points
 - ↳ preemption points chosen to minimize the CRPD

➤ Bertogna et al., "Optimal selection of preemption points to minimize preemption overhead"

Schedulability



- Fixed Preemptive Points
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Scheduling decisions are not directly based on a CRPD parameter.

Scheduling problems

- 1 Related work
- 2 Scheduling problems
 - CRPD-aware scheduling problem
 - Cache-aware scheduling problem
- 3 Conclusion
 - Future works

General approach

- **cache impact** on the computational complexity of *optimally* taking **scheduling decisions**

General approach

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General approach

- **cache impact** on the computational complexity of *optimally* taking **scheduling decisions**
 - 2 basic scheduling problems
 - ↳ to cover the largest set of scheduling problems
 - scheduling with *cache-related preemption delays*
 - **CRPD-aware scheduling problem**
 - scheduling with *cache state information*
 - **Cache-aware scheduling problem**

Computational complexity

➤ problem **classification**

↪ **time** needed **to solve** problem instances of arbitrary size

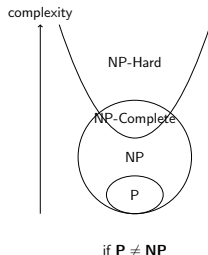
Computational complexity

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➤ complexity classes:

- **NP-hard** in the *weak sense*
 - ↪ at least *pseudo-polynomial time* algorithm
- **NP-hard** in the *strong sense*
 - ↪ at least *exponential time* algorithm



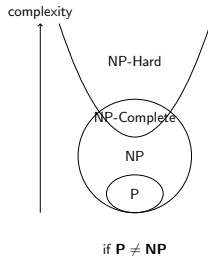
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➤ proof technique → polynomial reduction from a NP-complete problem



CRPD-aware scheduling problem

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CRPD-aware scheduling problem

Scheduling decisions taken based on cache-related preemption costs
→ **minimize the general overhead.**

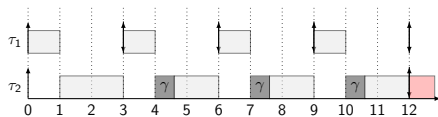
Task model: $\tau_i(C_i, D_i, T_i, \gamma)$

- C_i : WCET without preemption cost
↳ τ_i executed fully non preemptively
- γ : CRPD for one preemption
↳ the same for all program points and all tasks

Example: $\tau_1(1, 3, 3, 0.6)$, $\tau_2(7, 12, 12, 0.6)$

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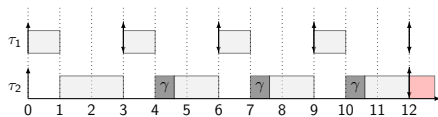
- Fixed-Task/Fixed-Job Priority Scheduling:



→ not schedulable

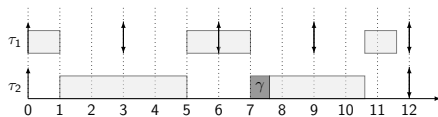
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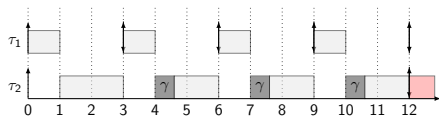
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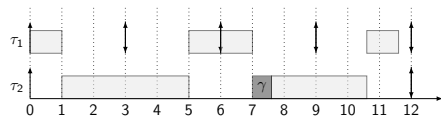
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- Fixed-Task/Fixed-Job Priority Scheduling:



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- CRPD-aware scheduling:



→ schedulable

⇒ Fixed-Task and Fixed-Job Priority schedulers → **not optimal.**

Complexity result

Finite set of tasks $\tau_i(C_i, D_i, T_i, \gamma)$,

↔ a uniprocessor preemptive schedule meeting the deadlines?

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Finite set of tasks $\tau_i(C_i, D_i, T_i, \gamma)$,

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⇒ **NP-hard** in the
strong sense.

Proof: transformation from the 3-Partition decision problem.

Cache-aware scheduling problem

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Cache-aware scheduling problem

Scheduling with cache state information

→ **maximize block reuse** by the different tasks.

↔ for only 1 task: Bélády's rule → optimal offline caching policy

Assumptions:

- a single cache line,
- synchronous jobs.

Job model: $J_i(C_i, D, S_i)$:

- C_i : WCET considering that all requested memory blocks are hits in the cache,
- D : relative deadline of the job → the same for all jobs,
- S_i : sequence of memory blocks used during the job execution
↔ no *if-then-else* structure

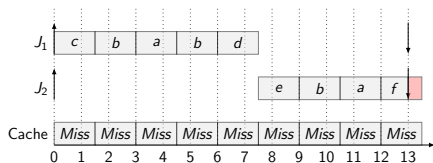
Example: $J_1(5, 13, cbabd)$, $J_2(4, 13, ebafe)$, Miss=Hit+0.5

$$S_1 = c \rightarrow b \rightarrow a \rightarrow b \rightarrow d, \quad S_2 = e \rightarrow b \rightarrow a \rightarrow f$$

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- Fixed-Job Priority Scheduling
($prio(J_1) > prio(J_2)$):

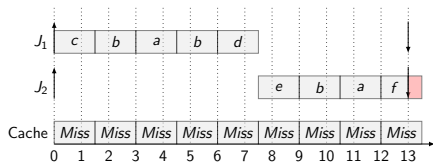


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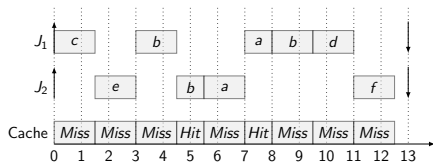
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- Cache-aware scheduling:

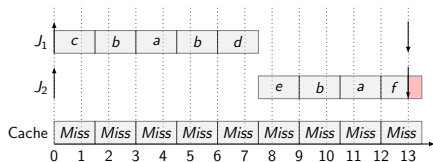


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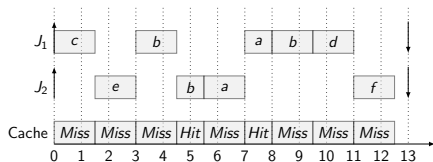
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→ not schedulable

- Cache-aware scheduling:



→ schedulable

⇒ Fixed-Task and Fixed-Job Priority schedulers → **not optimal.**

Complexity result

Finite set of n jobs $J_i(C_i, D, S_i)$ with a common deadline D
↔ a uniprocessor preemptive schedule meeting the overall deadline D for every job J_i ?

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Finite set of n jobs $J_i(C_i, D, S_i)$ with a common deadline D

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Proof: transformation from the Shortest Common Supersequence problem.

Conclusion & Future work

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Conclusion

- problem of **real-time scheduling** when dealing with **cache**

- *Cache-aware* scheduling problem
 - ↪ RM, EDF not optimal
 - ↪ **NP-hard** in the strong sense
 - ⇒ no pseudo-polynomial optimal scheduling algorithm

- *CRPD-aware* scheduling problem
 - ↪ RM, EDF not optimal
 - ↪ **NP-hard** in the strong sense
 - ⇒ no pseudo-polynomial optimal scheduling algorithm

Future work

Focus on the CRPD-aware scheduling problem

- use a simple (γ_i) linear programming to find an optimal solution → *will be presented at RNTS'2015*
- evaluate the loss of schedulability of different scheduling policies when CRPD are considered
 - Rate-Monotonic, EDF...
 - Preemption Thresholds, Deferred Preemptions

Thank you!
Questions?