

# Interactions between WCET analysis and scheduling

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## 1 Introduction

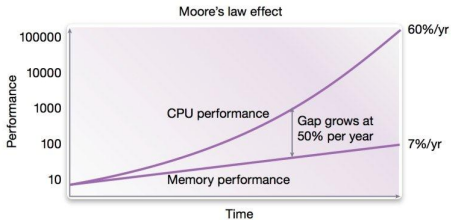
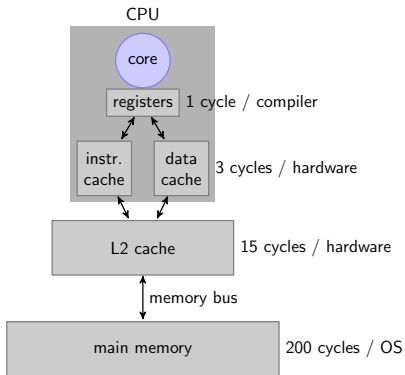
## 2 Context

- Into the WCET
- Into the scheduling analysis
- Reducing CRPD

## 3 Contributions

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- Problem 1: CRPD-aware scheduling
- Problem 2: Cache-aware scheduling

## 4 Conclusion



## Cache

Small and fast memory (compared to the main memory).

→ to bridge the gap between the processor speed and the main memory access time.

→ by storing:

- data that is frequently accessed (temporal locality),
- data that will (or may) be accessed next (spatial locality).

Instruction vs data caches, shared cache, cache hierarchy...

When a block is accessed:

- in cache: **cache hit** → low cost ( $\approx 1$  to 4 clock cycles),
- not in cache: **cache miss** → high cost ( $\approx 8$  to 32 cycles).

# Cache organization

Cache:

- divided into **cache lines** of equal size:
  - number of contiguous bytes transferred from the main memory to the cache.
- that may be grouped into sets:
  - **direct-mapped**: 1 line = 1 set
    - a memory block can be mapped to only *one line*.
  - **fully-associative**: only one set containing all lines
    - a memory block can be mapped *everywhere* in the cache.
  - **set-associative**: lines equally divided into several sets
    - a memory block can be mapped only to *one set* BUT everywhere in it.

Eg: 8kB direct-mapped instruction cache with a 8 bytes line size and a 4 bytes instruction size (ARM7).

# Replacement policy

## Offline:

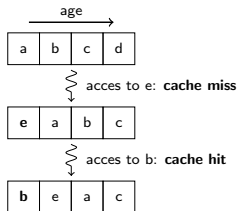
Belady's rule: the block whose next request is the furthest in the future is evicted.  $\Rightarrow$  OPTIMAL.

## Online:

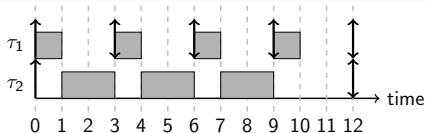
No optimal policy, as the access sequence is not known.

- LRU: Least Recently Used.

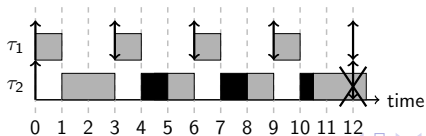
Example with a 4-way associative cache set



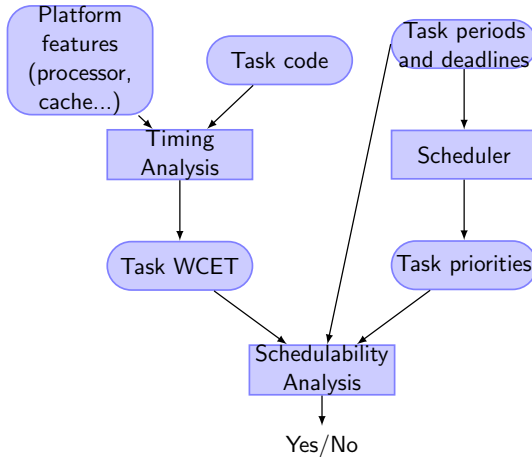
# Cache-Related Preemption Delay (CRPD)



adding  
preemption  
costs



# Classical approaches





# "Magic" WCET

Goal:

- WCET accounting for all potential preemption delays.
  - preemption costs have no longer to be considered into the scheduling analysis.



# Magic WCET: Approach 1

Easiest way to incorporate preemption delays into the WCET:

- **every access** → considered to be a **cache miss** (as if the cache was disabled)

But very pessimistic, and cache benefits are not taking any more into account.

## Magic WCET: Approach 2

- taking cache benefits into account  $\rightarrow$  tighter WCET,
- upper-bounding cache effects (**CRPD**: Cache-Related Preemption Delays)  $\rightarrow$  to achieve predictability.

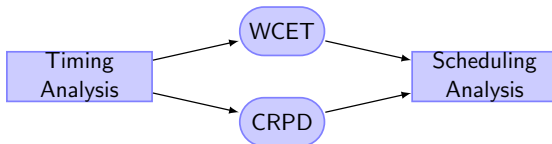
$\rightarrow$  by conducting cache analyses:

- 1 for WCET: representation of cache contents to identify accesses that will be "**Always Hits**".
- 2 to bound the impact of a preemption at a given program point.

$$\underbrace{WCET_{w/o \text{ preemption}}}_{(1)} + n \cdot \underbrace{CRPD}_{(2)}$$

Problem: how to get  $n$ ?  $\rightarrow$  very dependant on the chosen scheduling policy and the considered task system.

# CRPD incorporated into the scheduling analysis



$$R_i = C_i + \sum_{\forall j \in hp(i)} \left\lceil \frac{R_j}{T_j} \right\rceil \cdot \left( C_j + \underbrace{\gamma_{i,j}}_{\text{CRPD parameter}} \right)$$

$hp(i)$  : tasks of higher priority than task  $\tau_i$ .

$\gamma_{i,j}$  : preemption cost due to each job of a higher priority preempting task  $\tau_j$  executing within the worst-case response time of task  $\tau_i$ .

## Controlling preemption

Using well-known scheduling policies such as RM or EDF, schedulability improvement can be achieved by:

- limiting preemptions (*Buttazzo et al. 2013*),
- selecting the best possible preemption points in the program code, based on their overhead cost (*Bertogna et al. 2011*),
- ...

⇒ reduce CRPD.

But, scheduling decisions are independent from any cache-related parameter.

All previous strategies → use of "classical" scheduling policies (RM, EDF...):

- CRPD added to achieve better predictability,
- **but** scheduling decisions are independant from any cache-related parameter.

Would it not be better to take scheduling decisions to reduce CRPD?

- Taking delays due to the use of caches into account in the definition of scheduling algorithms.
  - Task model modified → addition of cache-related parameters:
    - ① representing the sequence of accessed block,
    - ② representing preemption cost.

# CRPD-aware scheduling

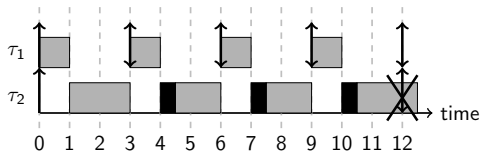
Scheduling decisions taken based on preemption costs  $\rightarrow$  to minimize the general overhead.

Task defined by  $\tau_i(C_i, D_i, T_i, \gamma)$

- $C_i$ : WCET without preemption cost estimated when  $\tau_i$  is executed fully non preemptively,
- $\gamma$ : CRPD for one preemption  $\rightarrow$  the same for all program points and all tasks.

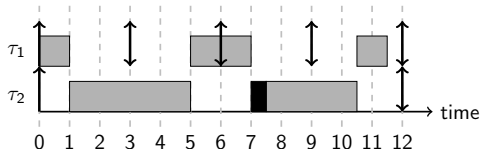
$\tau_1(1, 3)$ ,  $\tau_2(7, 12)$ , CRPD:  $\gamma = 0.5$ .

- Fixed-Job Priority Scheduling:



⇒ Fixed-Task and Fixed-Job Priority schedulers are **not optimal**.

- CRPD-aware scheduling:





## Simplified scheduling with CRPD problem:

- INSTANCE:
  - a finite set of  $n$  tasks  $\tau_i(C_i, D_i, T_i)$ ,
  - a positive number  $\gamma$  representing the Cache-Related Preemption Delay incurred by  $\tau_i$ ,  $1 \leq i \leq n$  at every resume point after a preemption.
- QUESTION:
  - Is there a uniprocessor preemptive schedule meeting the deadlines?

⇒ the scheduling problem with CRPD is **NP-hard**.

# Cache-aware scheduling

Scheduling with information about cache state and block reuse by the different tasks.

- eg: tasks using the same data or a common external library.

Job defined by  $J_i(C_i, D_i, S_i)$ :

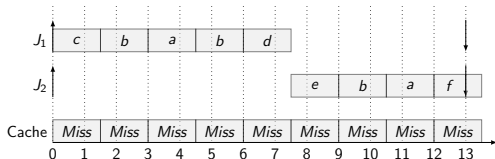
- $C_i$ : WCET considering that all requested memory blocks are hits in the cache,
- $D_i$ : relative deadline of the job,
- $S_i$ : string denoting the sequence of memory blocks used during the job execution (no *if-then-else* structure).

Hypotheses:

- a single cache line,
- hit cost = 0, miss cost =  $BRT$  (Block Reload Time),
- job preemption  $\rightarrow$  only before requesting the next block,
- synchronous jobs.

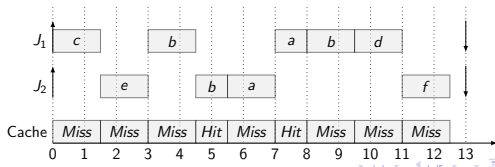
Cache size = 1, exec.(hit) = 1, exec.(miss) = 1.5,  $S_1 = cbabd$ ,  
 $S_2 = eba f$ .

- Fixed-Job Priority Scheduling ( $prio(J_1) > prio(J_2)$ ):



⇒ Fixed-Task and Fixed-Job Priority schedulers are **not optimal**.

- Cache-aware scheduling:

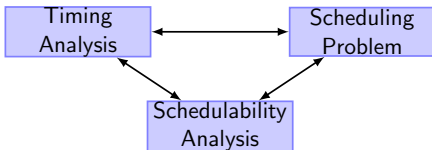


## Simplified scheduling with cache memory problem:

- INSTANCE:
  - a finite alphabet  $\Sigma \rightarrow$  representing all accessed blocks,
  - a finite set of  $n$  jobs  $J_i(C_i, D, S_i)$  with a common deadline  $D$ ,
- QUESTION:
  - Is there a uniprocessor preemptive schedule meeting the overall deadline  $D$  for every job  $J_i$ ?

⇒ the scheduling problem with cache memory is **NP-hard**.

# Conclusion



Improving WCET  $\Rightarrow$  make scheduling more complex.

Many questions:

- which task(s) model(s)?
- which parameters for the timing analysis (WCET, CRPD...)?
- ...

**Thank you for you attention!**